

Bruchgleichungen lösen

Lösungsblatt

$$\begin{aligned}
 1. \quad & \frac{x+2}{2} - 3 = \frac{x+2}{7} \quad / \cdot 14 \\
 & (x+2) \cdot 7 - 3 \cdot 14 = (x+2) \cdot 2 \\
 & 7x + 14 - 42 = 2x + 4 \\
 & 7x - 28 = 2x + 4 \quad / - 2x \\
 & 5x - 28 = 4 \quad / + 28 \\
 & 5x = 32 \quad / : 5 \\
 & \underline{x = 6,4}
 \end{aligned}$$

Probe: $x = 6,4$

$$\begin{aligned}
 & \frac{x+2}{2} - 3 = \frac{x+2}{7} \\
 & \frac{6,4+2}{2} - 3 = \frac{6,4+2}{7} \\
 & 4,2 - 3 = 1,2 \\
 & \underline{1,2 = 1,2 ; w. A}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & \frac{4-x}{x-6} - \frac{48}{x^2-36} = \frac{1-x}{x+6} \quad / \cdot (x^2-36) \\
 & (4-x) \cdot (x+6) - 48 = (1-x) \cdot (x-6) \\
 & 4x - x^2 + 24 - 6x - 48 = x - x^2 - 6 + 6x \\
 & -x^2 - 2x - 24 = -x^2 + 7x - 6 \quad / + x^2 \\
 & -2x - 24 = 7x - 6 \quad / + 2x \\
 & -24 = 9x - 6 \quad / + 6 \\
 & -18 = 9x \quad / : 9 \\
 & \underline{x = -2}
 \end{aligned}$$

Probe: $x = -2$

$$\begin{aligned}
 & \frac{4-(-2)}{(-2)-6} - \frac{48}{(-2)^2-36} = \frac{1-(-2)}{(-2)+6} \\
 & \frac{6}{-8} - \frac{48}{-32} = \frac{3}{4} \quad / \cdot 32 \\
 & -(6 \cdot 4) + 48 = 24 \\
 & \underline{24 = 24 ; w. A}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad & \frac{x+4}{x^2-1} = \frac{5}{x-1} - \frac{3}{x+1} \quad / \cdot (x^2-1) \\
 & x+4 = 5 \cdot (x+1) - 3 \cdot (x-1) \\
 & x+4 = 5x+5-3x+3 \\
 & x+4 = 2x+8 \quad / - x \\
 & 4 = x+8 \quad / - 8 \\
 & \underline{x = -4}
 \end{aligned}$$

Probe: $x = -4$

$$\begin{aligned}
 & \frac{(-4)+4}{(-4)^2-1} = \frac{5}{(-4)-1} - \frac{3}{(-4)+1} \\
 & \frac{0}{15} = \frac{5}{(-4)-1} - \frac{3}{(-4)+1} \\
 & 0 = -1 + 1 \\
 & \underline{0 = 0 ; w. A}
 \end{aligned}$$

$$\begin{aligned}
 4. \quad & \frac{x+2}{4x+14} = \frac{x-2}{4x+2} \quad / \cdot (4x+14) \cdot (4x+2) \\
 & (x+2) \cdot (4x+2) = (x-2) \cdot (4x+14) \\
 & 4x^2 + 8x + 2x + 4 = 4x^2 - 8x + 14x - 28 \quad / - 4x^2 \\
 & 10x + 4 = 6x - 28 \quad / - 6x \\
 & 4x + 4 = -28 \quad / - 4 \\
 & 4x = -32 \quad / : 4 \\
 & \underline{x = -8}
 \end{aligned}$$

Probe: $x = -8$

$$\begin{aligned}
 & \frac{(-8)+2}{4 \cdot (-8) + 14} = \frac{(-8)-2}{4 \cdot (-8) + 2} \\
 & \frac{-6}{-18} = \frac{-10}{-30} \\
 & \underline{3 = 3 ; w. A}
 \end{aligned}$$